

Acoustical Characterization of Gunshots

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Outline

- Applications
- Gunshot acoustical properties
 - Mechanical action
 - Muzzle blast
 - Shock wave (supersonic projectiles)
- Range effects
 - Propagation and Attenuation
 - Reflections
 - Limitations
- Conclusions

Gunshot Analysis Applications

- Real Time Tactical Information
 - Gunshot Detection
 - Sniper Localization
- Forensic Reconstruction
 - Timeline Assessment
 - Shooter Location and Orientation
 - Firearm Classification

Sound Characteristics



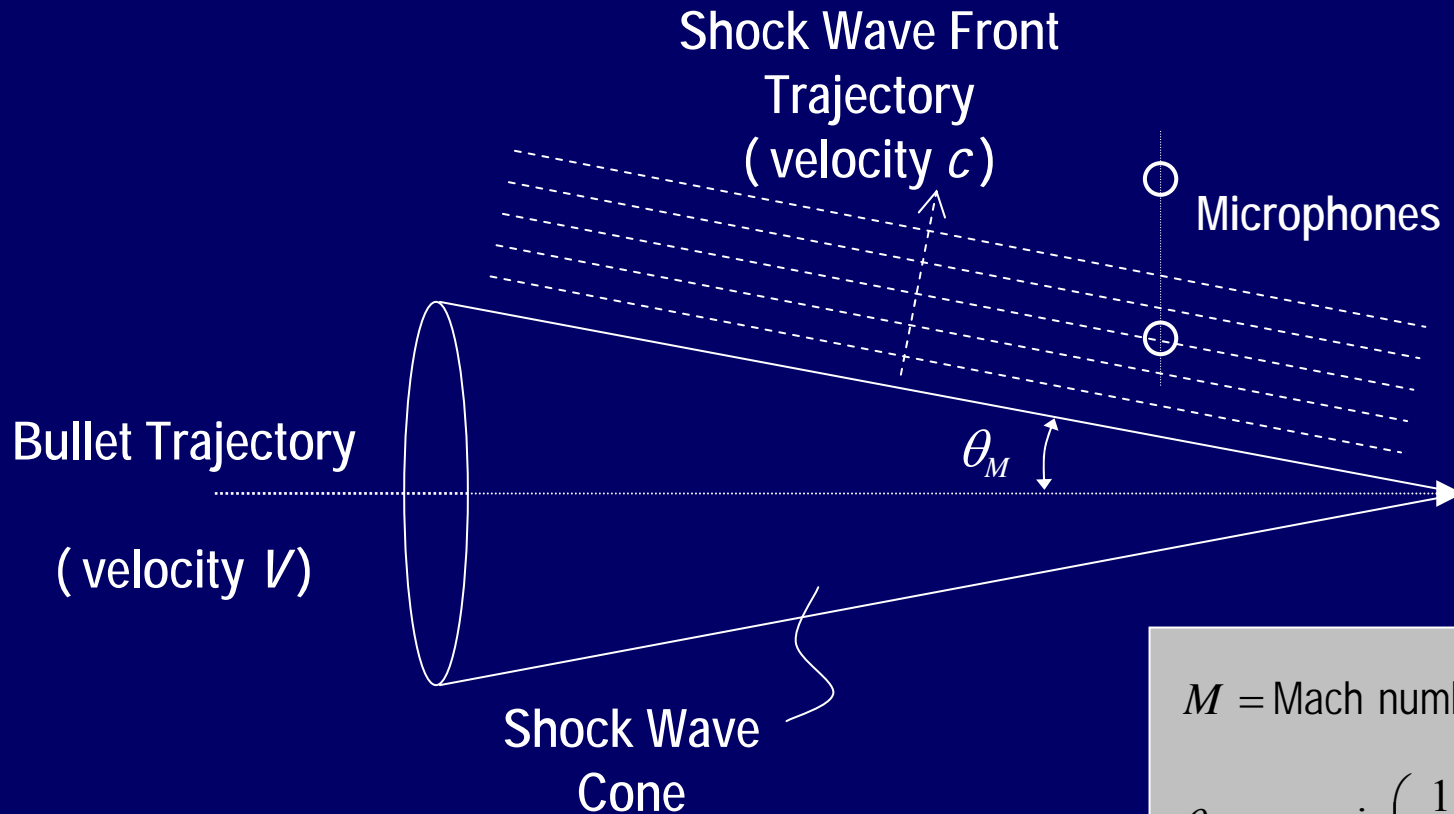
- Acoustic behavior depends upon:
 - Firearm type
 - Projectile parameters
 - Explosive load
 - Distance
 - Meteorology
 - Obstacles



Acoustical Gunshot Evidence

- Mechanical Action
- Muzzle Blast
- Supersonic Projectile (shock wave)
- Surface Vibration
- Reflections, Refraction, Reverberation
- Microphone Type and Location
- Audio Coding Issues (e.g., cell phone)

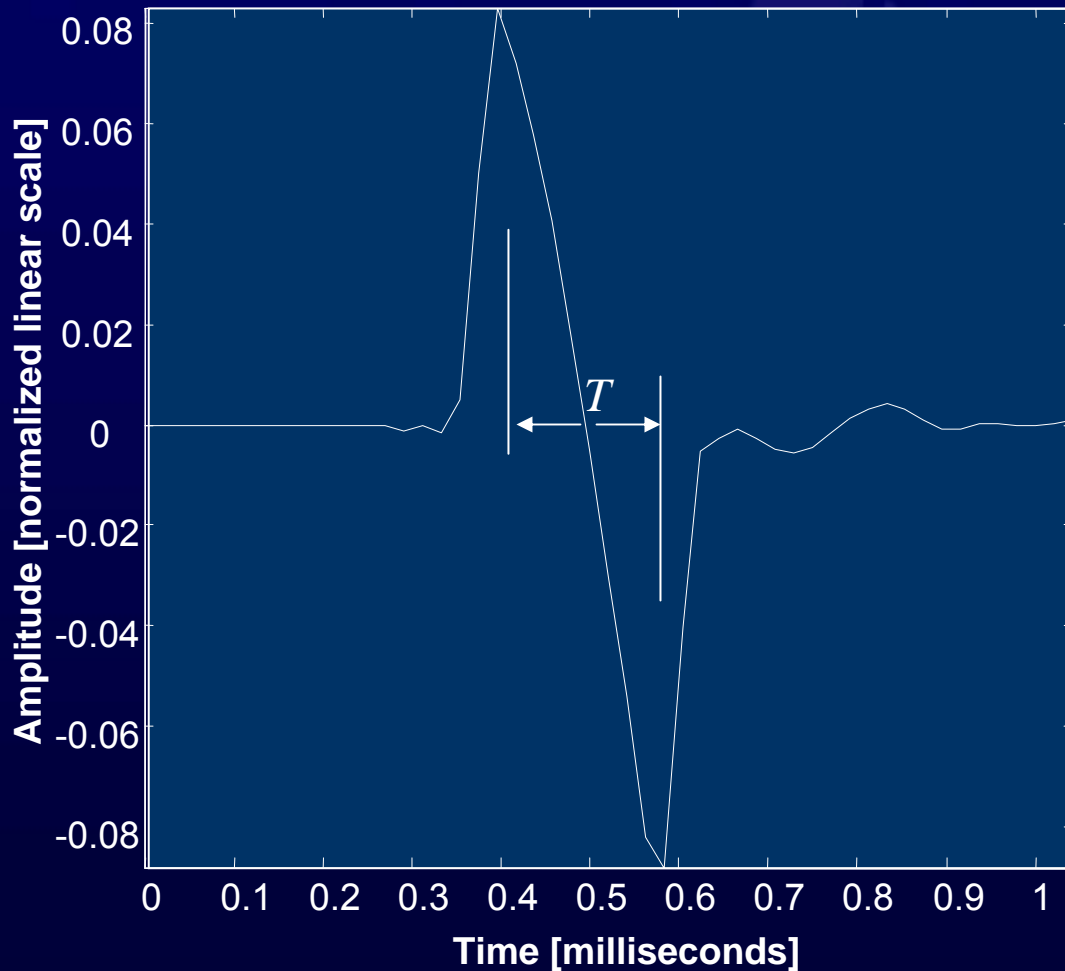
Supersonic Projectile



$$M = \text{Mach number} = \frac{V}{c}$$

$$\theta_M = \arcsin\left(\frac{1}{M}\right)$$

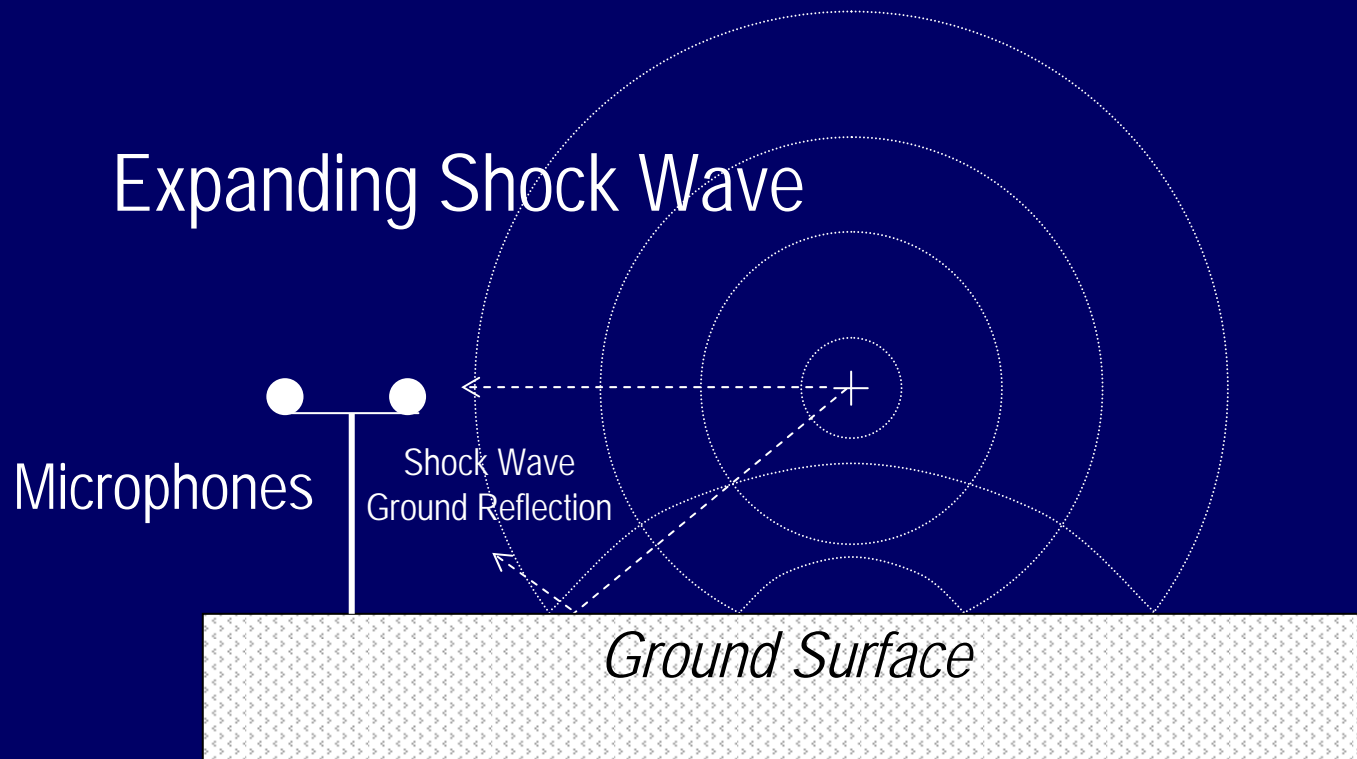
'N' Shaped Shock Wave



$$T \approx 1.82 \left(\frac{d}{c} \right) \left(\frac{Mx}{l} \right)^{\frac{1}{4}}$$

d = bullet diameter
 c = speed of sound
 M = Mach number
 x = path to microphone distance
 l = bullet length

Multipath: Ground Reflection



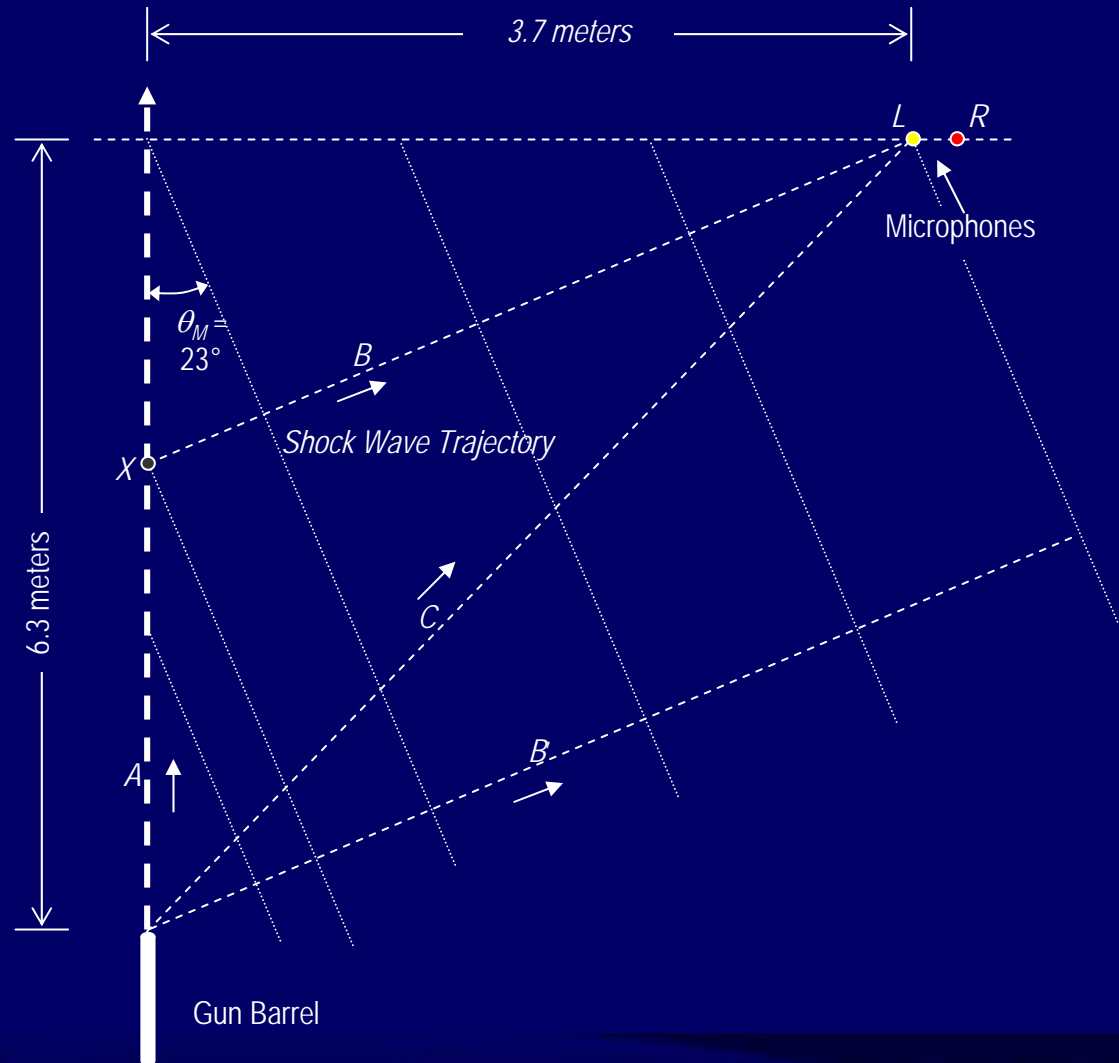
Shock Wave Timing Example

Bullet speed at muzzle:
2728 ft/sec (831.5 m/sec)

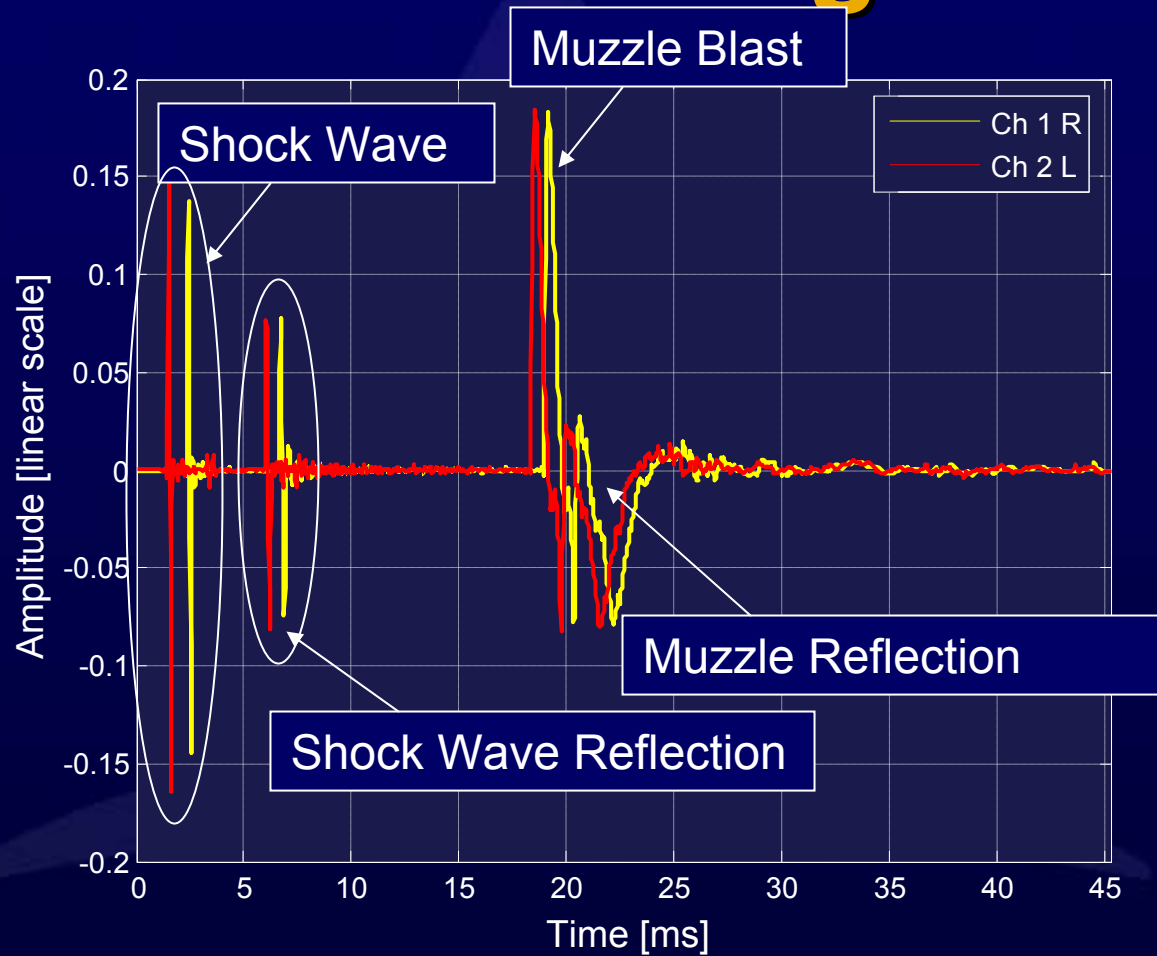
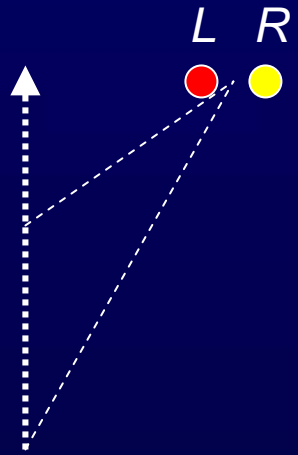
Speed of sound (c):
1075 ft/sec (328 m/sec)

Mach Number (V/c):
2.54

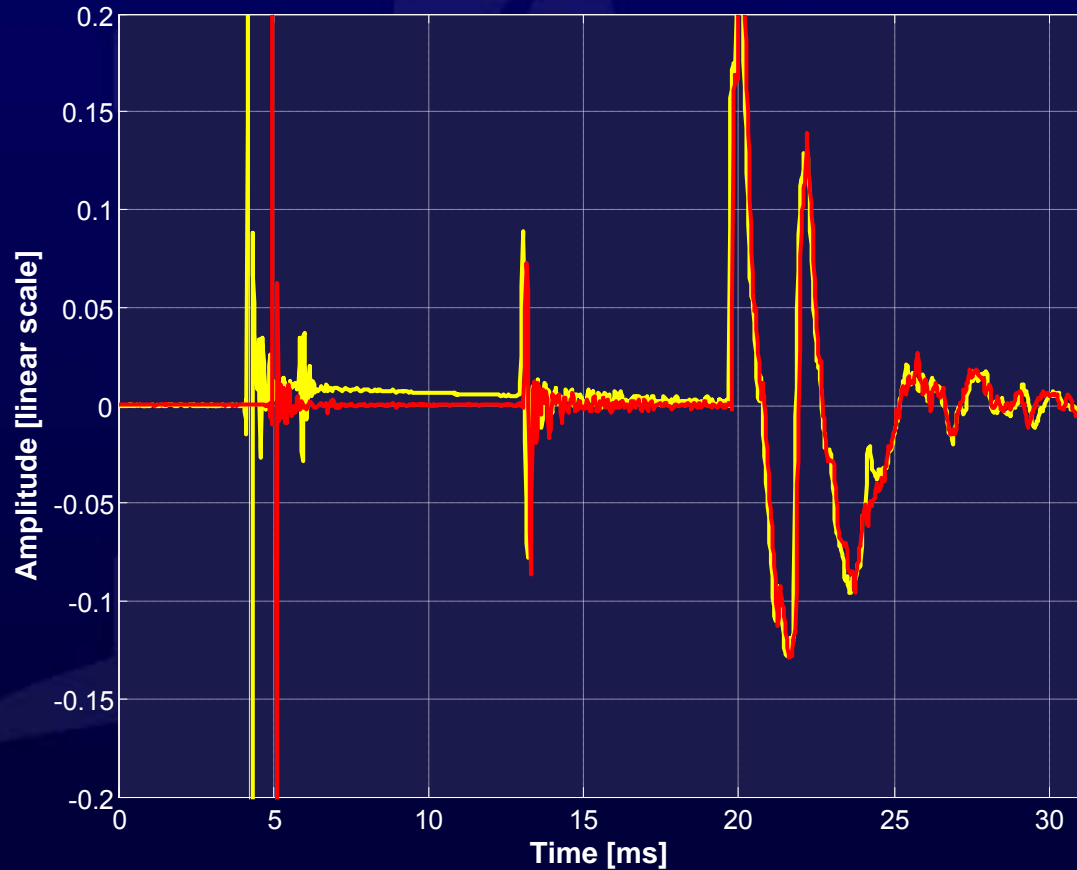
Mach Angle (θ_M):
 23.2°



Gunshot Recording: Path 1

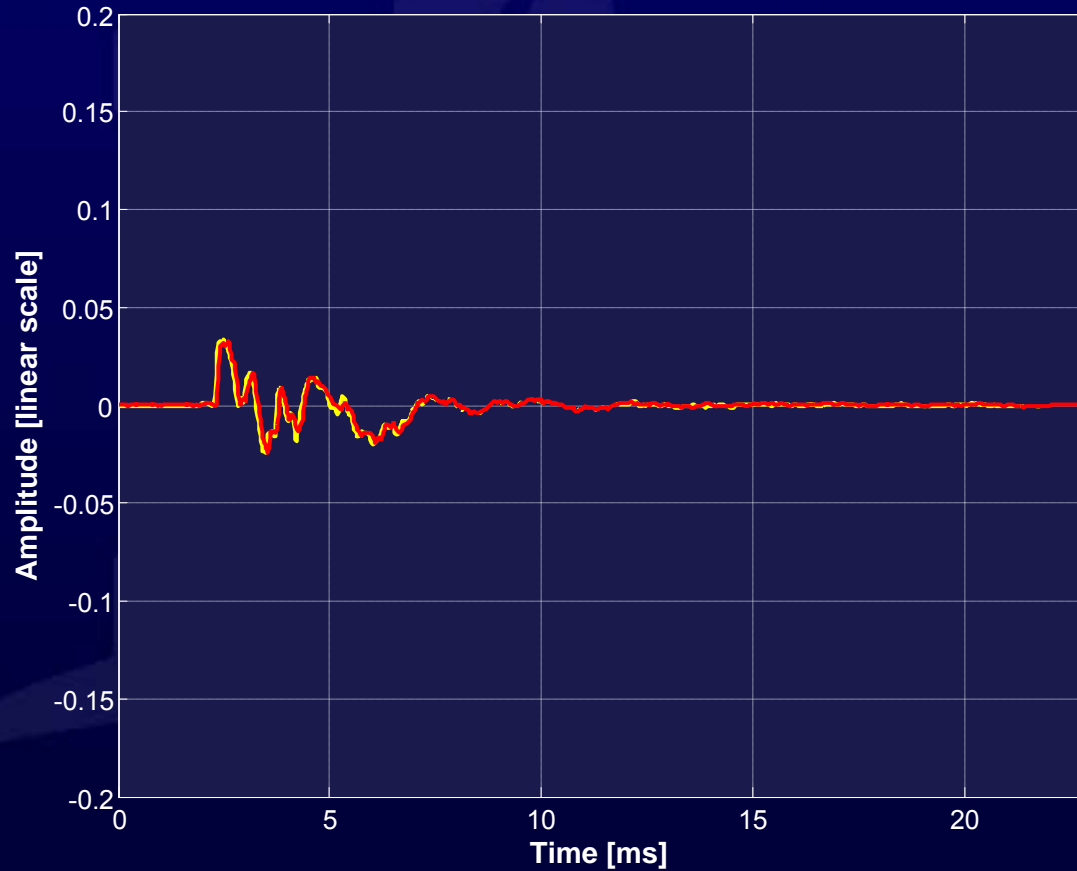


Gunshot Recording: Path 2

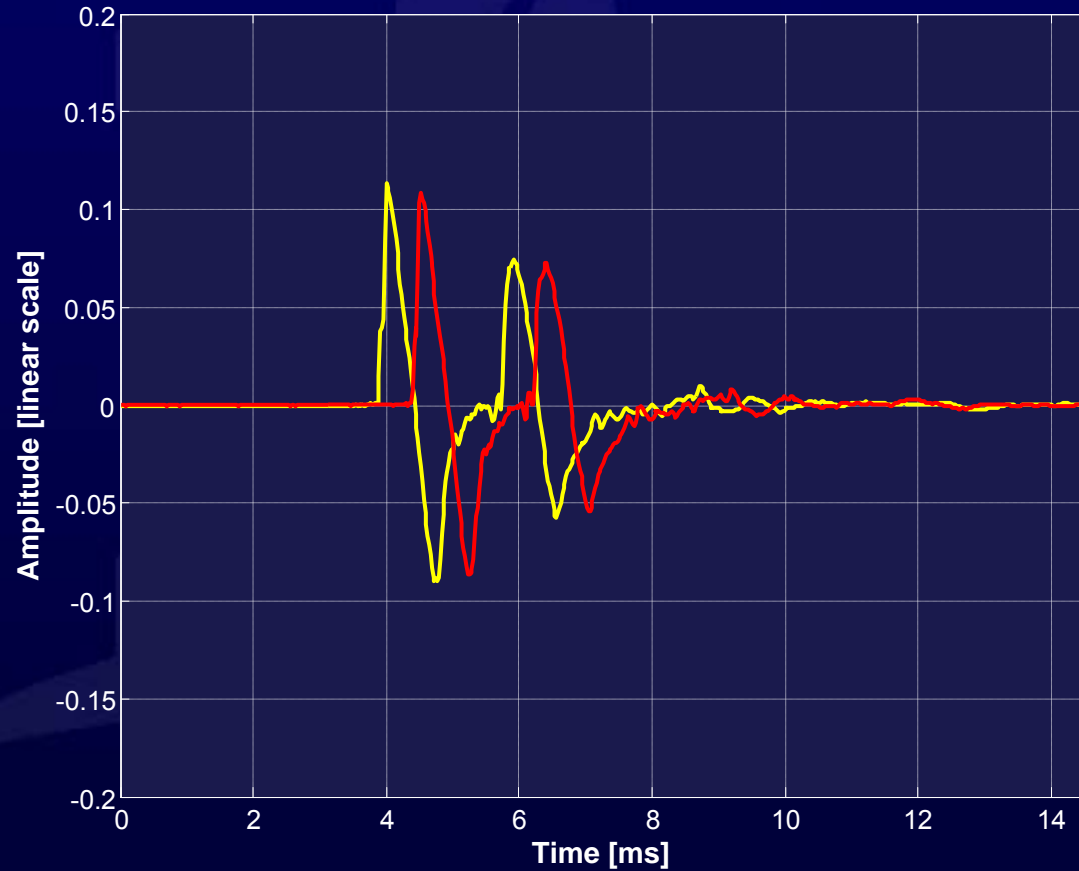
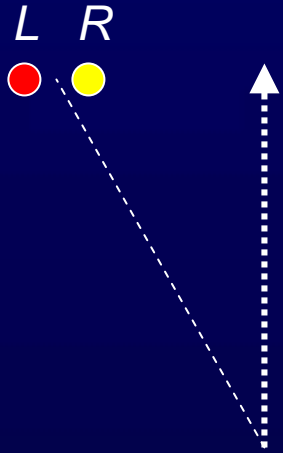


Gunshot Recording: Path 3

L R
● ●



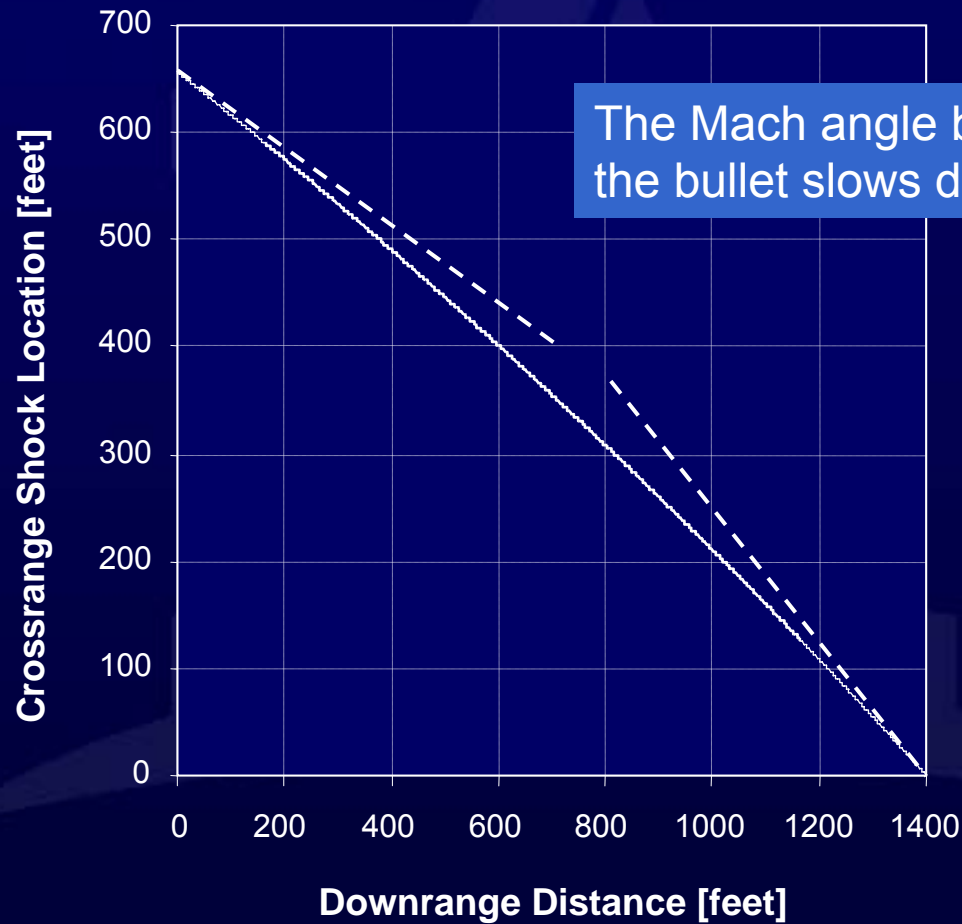
Gunshot Recording: Subsonic



Propagation Effects

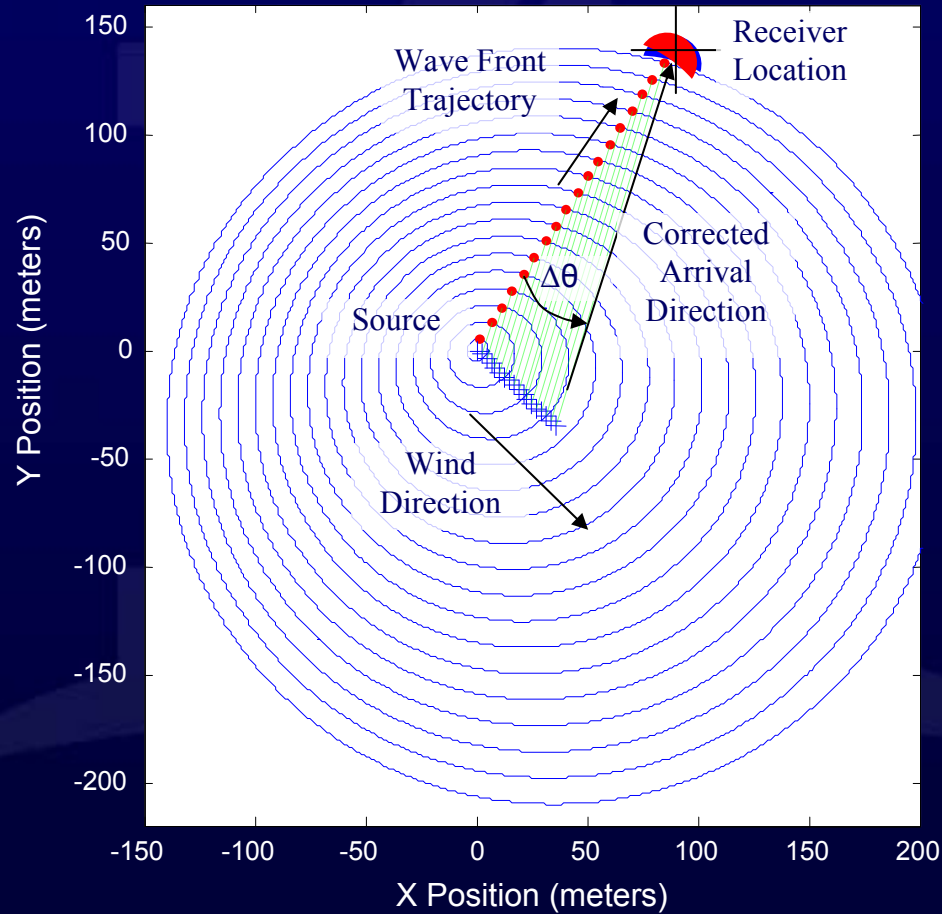
- Attenuation due to acoustical spreading
- Obstacles: reflection and diffraction
- Path elevation trajectory
- Projectile deceleration
- Temperature gradient
- Wind gradient

Projectile Deceleration



The Mach angle broadens as the bullet slows downrange

Effect of Wind



Effect of Temperature

- The speed of sound (c) in air increases with increasing temperature:

$$c = c_0 \sqrt{1 + \frac{T}{273}}$$

(T in $^{\circ}$ C and $c_0 = 331$ m/s)

- Hotter air near ground: curves upward
- Cooler air near ground: curves downward

Conclusion

- Closely-miked gunshot recordings:
 - Geometric acoustics works well
- Distant recordings:
 - Propagation effects lead to greater uncertainty due to altered sound path
 - Reflections and reverberation dominate
- Verification is needed to assess the validity of acoustic analysis claims