

(1) The drive element of a dynamic speaker is described by the following parameters:

mass (voice coil, cap, cone) ( $m$ ): 10 grams  
stiffness ( $s$ ): 1750 N/m  
damping ( $R_m$ ): 0.9 N·s/m

(a) Find the damped natural frequency ( $\omega_d$ ), the decay time constant ( $\tau$ ) and the mechanical resonant frequency ( $\omega_0$ ).

(b) Determine and sketch a plot of the mechanical impedance magnitude  $Z_m = \sqrt{R_m^2 + X_m^2}$  for an interesting range of frequency.

(2) A simple mechanical oscillator (i.e., negligible damping) has mass=0.5 kg. If the mass is displaced from its equilibrium position by 5 cm, the force required to hold it there is found to be 26 N.

The mass is released from its 5cm displacement, and triggers a clock when it passes the equilibrium position. In other words, the mass is at  $x=0$  when  $t=0$ , but its velocity is *not* zero at  $t=0$ .

(a) Find the natural oscillation frequency in Hz ( $f_0$ ), for the resulting oscillation.

(b) Find the mechanical stiffness ( $s$ ) of the system.

(c) Find the velocity ( $u_0$ ) at  $t=0$ .

(d) Find the mathematical expression for the displacement,  $x(t)$ , for  $t \geq 0$ .